



Lecture #2: Principles of Sensors

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**Some slides obtained from
12-740 for Fall 2006*

Civil & Environmental
ENGINEERING
Carnegie Mellon

12-778: Sensors, Circuits and Data Interpretation/Mgmt. for CEE

But first...

- Office Hours → Does this work?
 - Thursdays 10-11am
- Readings posted → Starting now, please read before class
- Equipment distribution -> Let's do it.

Recap

- Sensors, Actuators, Transducers?
- What physical phenomena can we sense to estimate indoor occupancy?

Additional Info

- <http://inferlab.github.io/12740/>
- Past projects:
 - <http://wiki.marioberges.com/courses/12-740/>
 - User: inspiration
 - Password: expiration

Agenda for today

Chapters 1 and 2 from Fraden

PRINCIPLES OF SENSORS

Instruments

- Instruments are devices we create to measure/estimate physical quantities of interest.
 - Transducers are but a component inside instruments.
- What you typically work with in practice are not just sensors, but instruments.

Instruments: what to know

- Transform physical stimulus to electrical signal
 - Designed for this purpose by combining different components
 - Tested
 - Response and drift are considered
 - Accuracy and errors are considered
 - They are (re-)calibrated
 - Could be analog or digital
 - Moving towards micro-instruments or virtual

LET'S DRAW SOME DIAGRAMS
OF INSTRUMENTS.

Definition of Sensor

Definition of Sensor:

- A device that receives and responds to a signal or stimulus.
- An electronic device that respond to some kind of an input physical property and convert it into an electrical signal which is compatible with electronic circuit.
- Sensor outputs can be in a form of voltage, current, or charge.

Sensor vs. Transducer:

- Transducer converts one type of energy into another form of energy. For example: a speaker that converts electrical signal into variable magnetic field, and into acoustic waves. Actuators are other examples.
- Sensor converts any type of energy into electrical signals.

Sensor Classifications

- Passive or Active
- Absolute or Relative
- By their characteristics:
 - Specifications
 - Materials
 - Detection Means
 - Conversion Phenomena
 - Application Area
 - Stimulus

Sensor Examples

- Accelerometer
- Fiber optic sensor
- Thermocouple
- Strain gauge
- Current Transformer

alog output CMOS integrated-circuit operates over a -55°C to $+130^{\circ}\text{C}$ power supply operating range is transfer function of LM20 is predictable parabolic curvature. When specified to a parabolic at an ambient temperature of $+30^{\circ}\text{C}$ increases linearly and reaches a temperature range extremes. The by the power supply voltage. At 2.7 V to 5.5 V the temperature and -55°C . Decreasing the power changes the negative extreme to mains at $+130^{\circ}\text{C}$.

ent is less than $10\text{ }\mu\text{A}$. Therefore, 2°C in still air. Shutdown capability cause its inherent low power consumed directly from the output of not necessitate shutdown at all.

- HVAC
- Disk Drives
- Appliances

Features

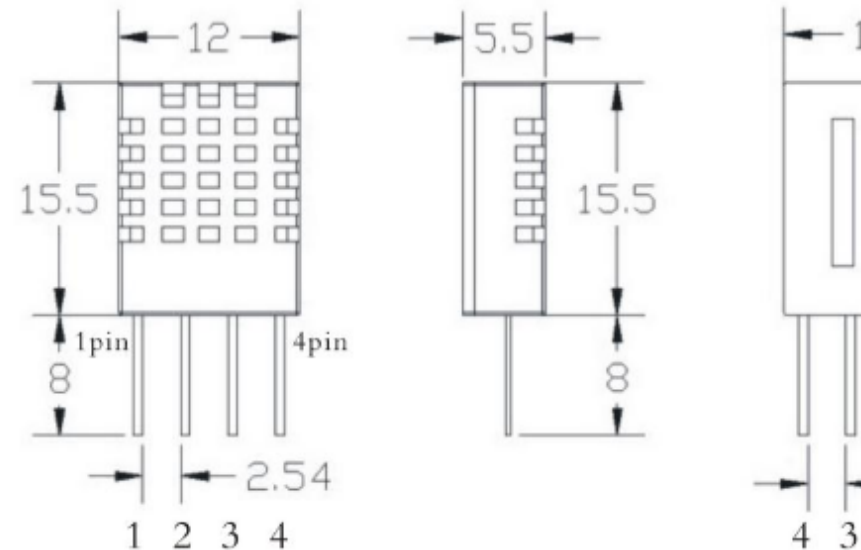
- Rated for full -55°C to $+130^{\circ}\text{C}$ range
- Available in an SC70 and micro SMD package
- Predictable curvature error
- Suitable for remote applications

Key Specifications

■ Accuracy at $+30^{\circ}\text{C}$	± 1.5 to $\pm 4\text{ }^{\circ}\text{C}$ (max)
■ Accuracy at $+130^{\circ}\text{C}$ & -55°C	± 2.5 to $\pm 5\text{ }^{\circ}\text{C}$ (max)
■ Power Supply Voltage Range	$+2.4\text{ V}$ to $+5.5\text{ V}$
■ Current Drain	$10\text{ }\mu\text{A}$ (max)
■ Nonlinearity	$\pm 0.4\text{ }\%$ (typ)
■ Output Impedance	$160\text{ }\Omega$ (max)
■ Load Regulation	
$0\text{ }\mu\text{A} < I_L < +16\text{ }\mu\text{A}$	-2.5 mV (max)

Your Temperature Sensor

Temperature and Humidity Module
DHT11



5. Parameters

Relative Humidity

Resolution : 16Bit

Repeatability : $\pm 1\%RH$

Accuracy : $25^{\circ}C$ $\pm 5\%RH$

Interchangeability : Fully interchangeable

Response time : $1/e$ (63%) $25^{\circ}C$ 6s

1m/s Air 6s

Humidity : $\pm 0.2\%RH$

Typical Accelerometer Data Sheet

Model Number 320C02	ACCELEROMETER, ICP®			Optional Versions (Optional for standard model except where noted)
Performance	ENGLISH	SI		J - Ground Isolated
Sensitivity (±10 %)	20 mV/g	2.04 mV/(m/s²)		Frequency Range (5 %)
Measurement Range	±250 g pk	±2452 m/s² pk		Frequency Range (10 %)
Frequency Range (±5 %)	1 to 6000 Hz	1 to 6000 Hz		Frequency Range (3 dB)
Frequency Range (±10 %)	0.7 to 9000 Hz	0.7 to 9000 Hz		Resonant Frequency
Frequency Range (±3 dB)	0.35 to 18000 Hz	0.35 to 18000 Hz		Electrical Isolation (Base)
Resonant Frequency	≥35 kHz	≥35 kHz		
Broadband Resolution (1 to 10000 Hz)	0.002 g rms	0.02 m/s² rms	[1]	
Non-Linearity	≤1 %	≤1 %	[2]	
Transverse Sensitivity	≤5 %	≤5 %	[3]	
Environmental				W - Water Resistant Cable
Overload Limit (Shock)	±7000 g pk	±68670 m/s² pk		Electrical Connector
Temperature Range (Operating)	-100 to +325 °F	-73 to +163 °C		
Temperature Response	See Graph	See Graph	[1]	Electrical Connection Position
Base Strain Sensitivity	≤0.0005 g/με	≤0.005 (m/s²)/με	[1]	Notes
Electrical				[1] Typical.
Excitation Voltage	18 to 30 VDC	18 to 30 VDC		[2] Zero-based, least-squares
Constant Current Excitation	2 to 20 mA	2 to 20 mA		[3] Transverse sensitivity
Output Impedance	≤100 ohm	≤100 ohm		[4] See PCB Declaration
Output Bias Voltage	8 to 12 VDC	8 to 12 VDC		
Discharge Time Constant	0.5 to 2.0 sec	0.5 to 2.0 sec		Supplied Accessories
Spectral Noise (10 Hz)	150 μg/√Hz	1472 (μm/s²)/√Hz	[1]	080A109 Petro Wax (1)
Spectral Noise (100 Hz)	30 μg/√Hz	294 (μm/s²)/√Hz	[1]	081B05 Mounting Stud (10-32)
Spectral Noise (1 kHz)	10 μg/√Hz	98 (μm/s²)/√Hz	[1]	ACS-1 NIST traceable frequency
Physical				M081B05 Mounting Stud 10-32
Sensing Element	Quartz	Quartz		
Sensing Geometry	Shear	Shear		
Housing Material	Titanium	Titanium		
Sealing	Welded Hermetic	(Welded Hermetic)		
Weight	0.38 oz	10.5 gm	[1]	
Electrical Connector	10-32 Coaxial Jack	10-32 Coaxial Jack		
Electrical Connection Position	Top	Top		

Accelerometer Applications

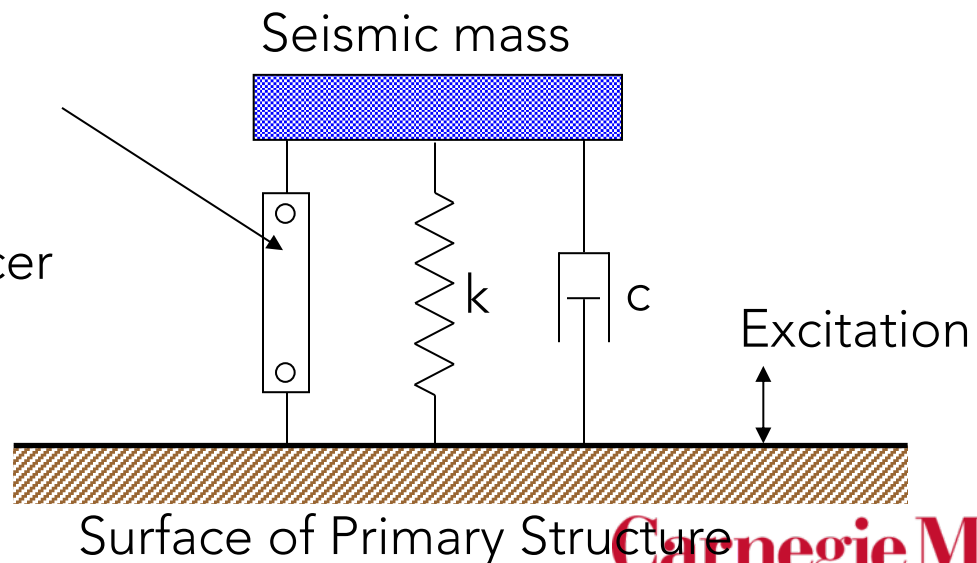
- Air Bag
- Navigation System
- Estimation of velocity and displacement
- Control systems
- And more...

Accelerometer Basics

- **Definition:** Accelerometers are electromechanical transducers used for measuring absolute acceleration.
- **Purpose:** Proper selection of accelerometers requires a fundamental understanding of an accelerometers' basic principles of operation.
- **Types:** two basic types of accelerometers are
 - Seismic accelerometers (a.k.a.: accelerometers)
 - Servo accelerometers (a.k.a.: force-balanced, inertial accelerometers)

Displacement Transducer

- Piezoelectric transducer
- Piezoresistance transducer
- Capacitance transducer



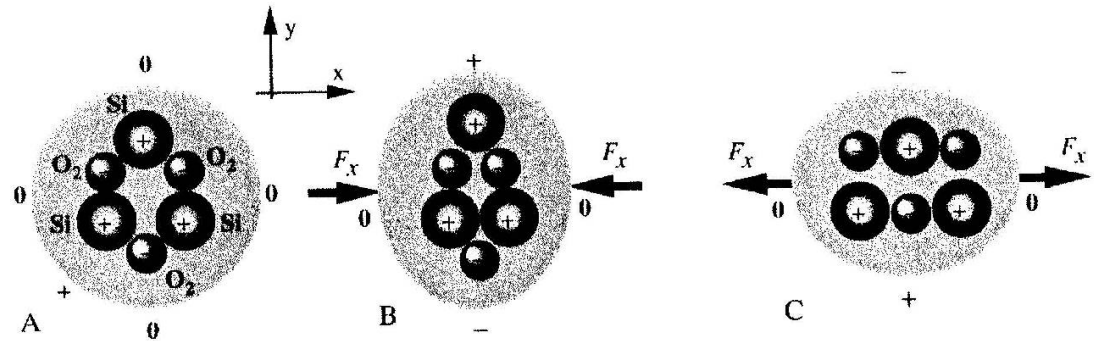
Piezoelectricity

- In piezoelectric materials such as quartz, the generated charge (Q) is proportional to the applied force (F):

$$Q = dF$$

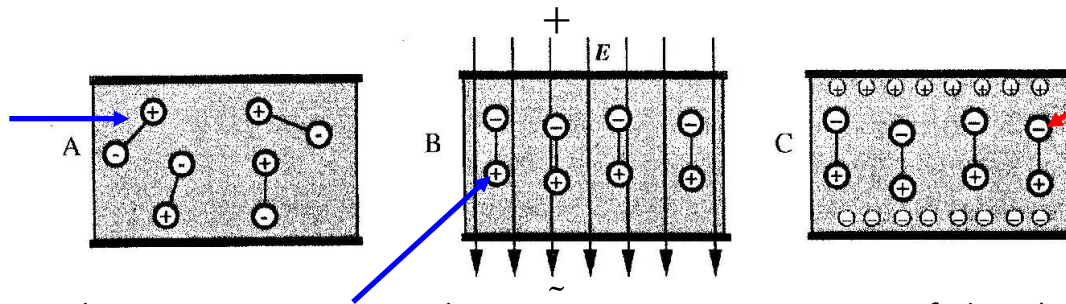
Piezoelectric coefficient

$$V = Q / C = \frac{dF}{C}$$



- Artificially polarized materials such as ceramics and some polymers can also be polarized to have the piezoelectric effect.

Crystalline materials have randomly oriented dipoles

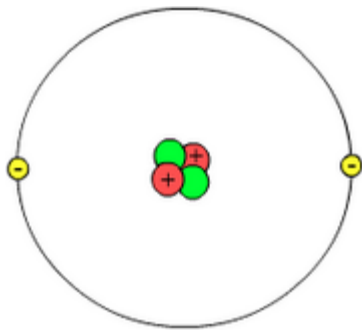


below the Curie temperature, their polarization remains permanent

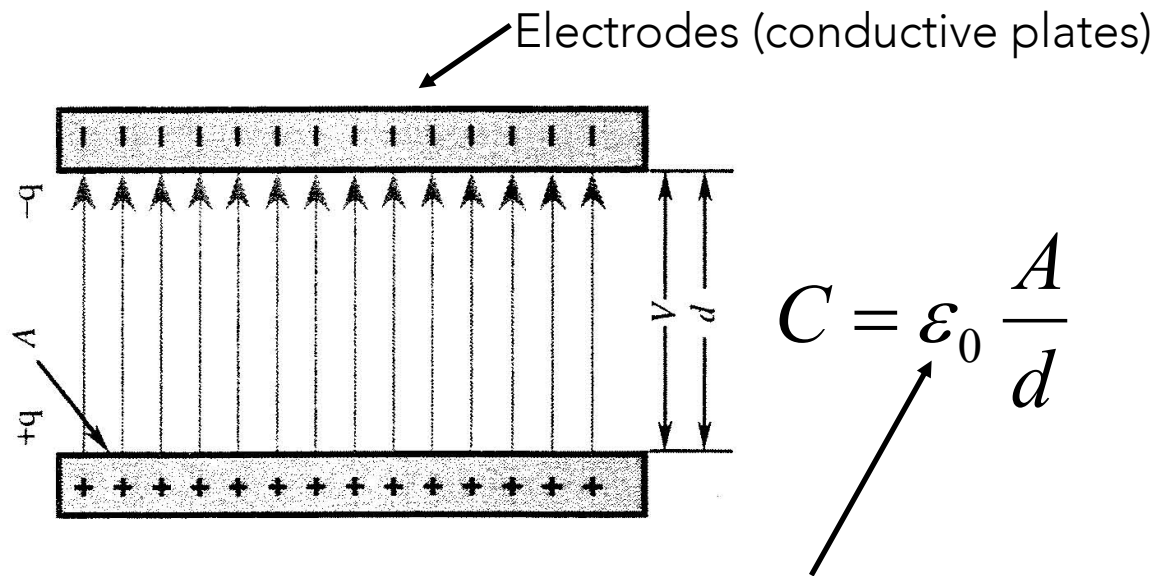
High temperature produces stronger agitation of dipoles and when they are subjected to electric field, they are aligned along the field lines

Capacitance

- C (i.e. Q/V) is a measure of the amount of electric charge stored for a given electric potential.
- $Q=CV$ where Q is charge in Coulombs, V is voltage in Volts, and C is capacitance in Farads.
- Electrons have a charge of $e=1.602 \times 10^{-19}$ Coulombs.



Helium atom
(schematic)
Showing two protons
(red), two neutrons
(green) and two
electrons (yellow).



Permittivity constant = $8.8542 \times 10^{-12} \text{ C}^2/\text{Nm}^2$

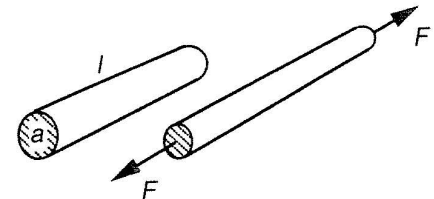
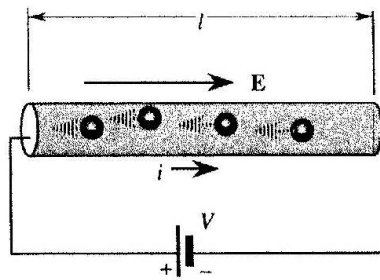
Resistance

- Electrical resistance is a measure of the opposition that a material imposes to electric current passing through it. ($R=V/i$)
- The resistance of the material is related to the cross section (a), length of the conductor (l) and the resistivity (ρ) of the material
- Electrical resistance changes when the material is mechanically deformed.

$$R = \rho \frac{l}{a} = \rho \frac{l^2}{v} \Rightarrow dR = 2\rho \frac{l}{v} dl$$

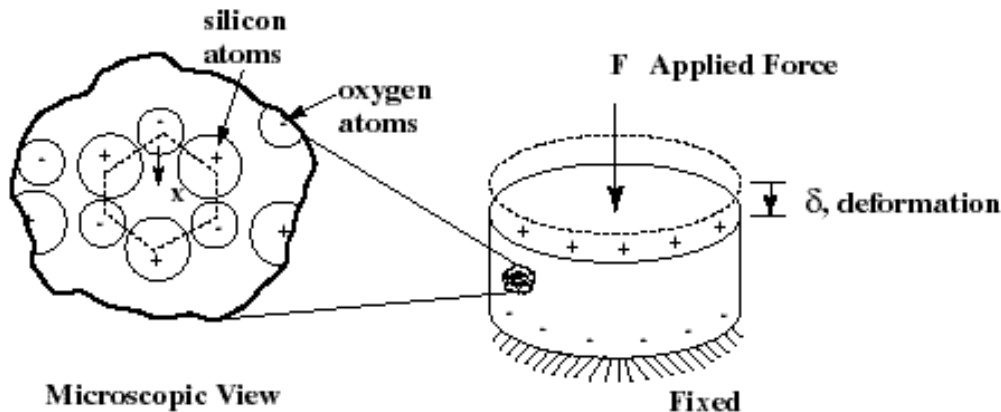
- The resistance is also related to temperature.

$$R = R_0[1 + \alpha(T - T_0)]$$

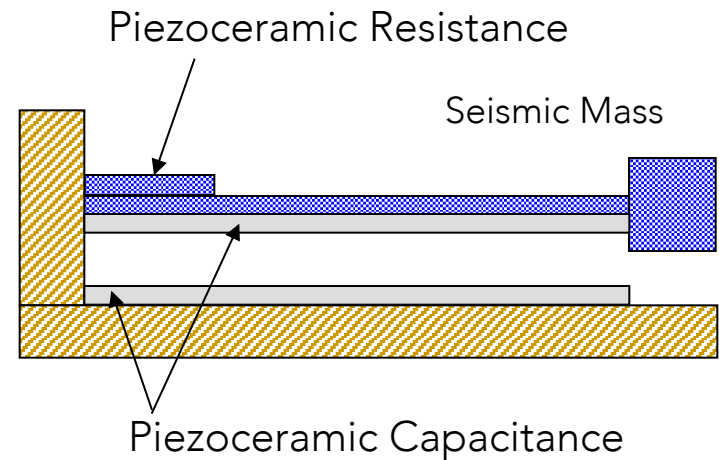


Different Displacement Transducers

- **Piezoelectric Transducer:** Charge is proportional to applied force and deformation. Good for a high frequency range. **Most commonly used for experimental modal analysis.**
- **Piezoresistance Transducer:** A change in resistance is proportional to imposed deformation. This type of accelerometer has excellent low frequency response down to DC level.
- **Capacitance Transducer:** The motion of the mass changes the capacitance of the capacitor.

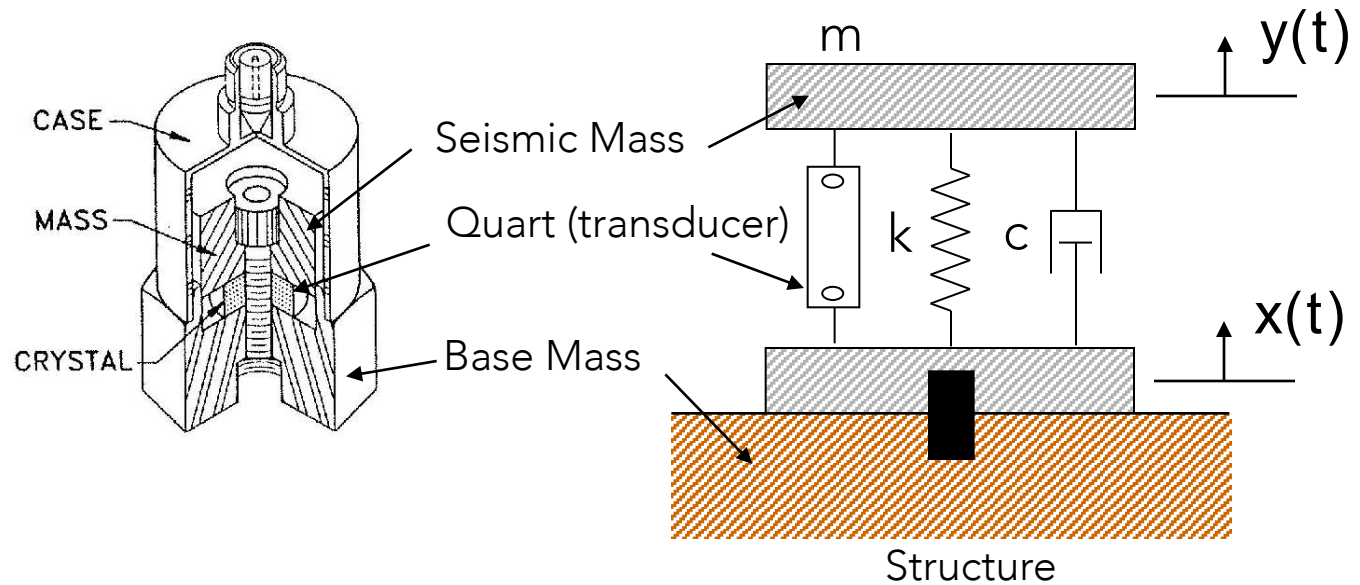


Piezoelectric Transducer



Piezoresistance or Capacitance Transducer

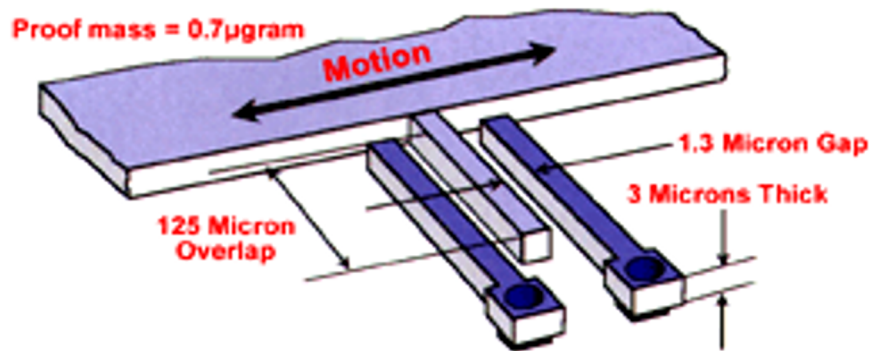
Piezoelectric Sensor



Define $z(t) = y(t) - x(t)$

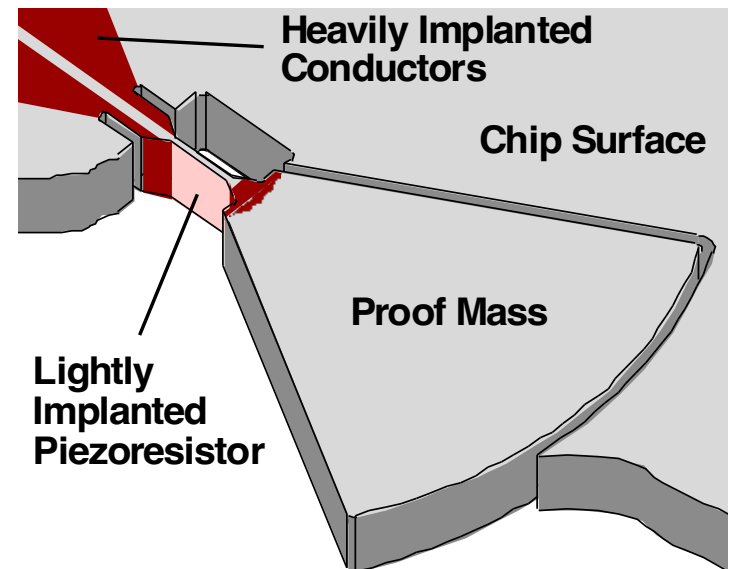
$$m\ddot{z}(t) + c\dot{z}(t) + kz(t) = -m\ddot{x}(t)$$

Piezocapacitive and Piezoresistive Accelerometers



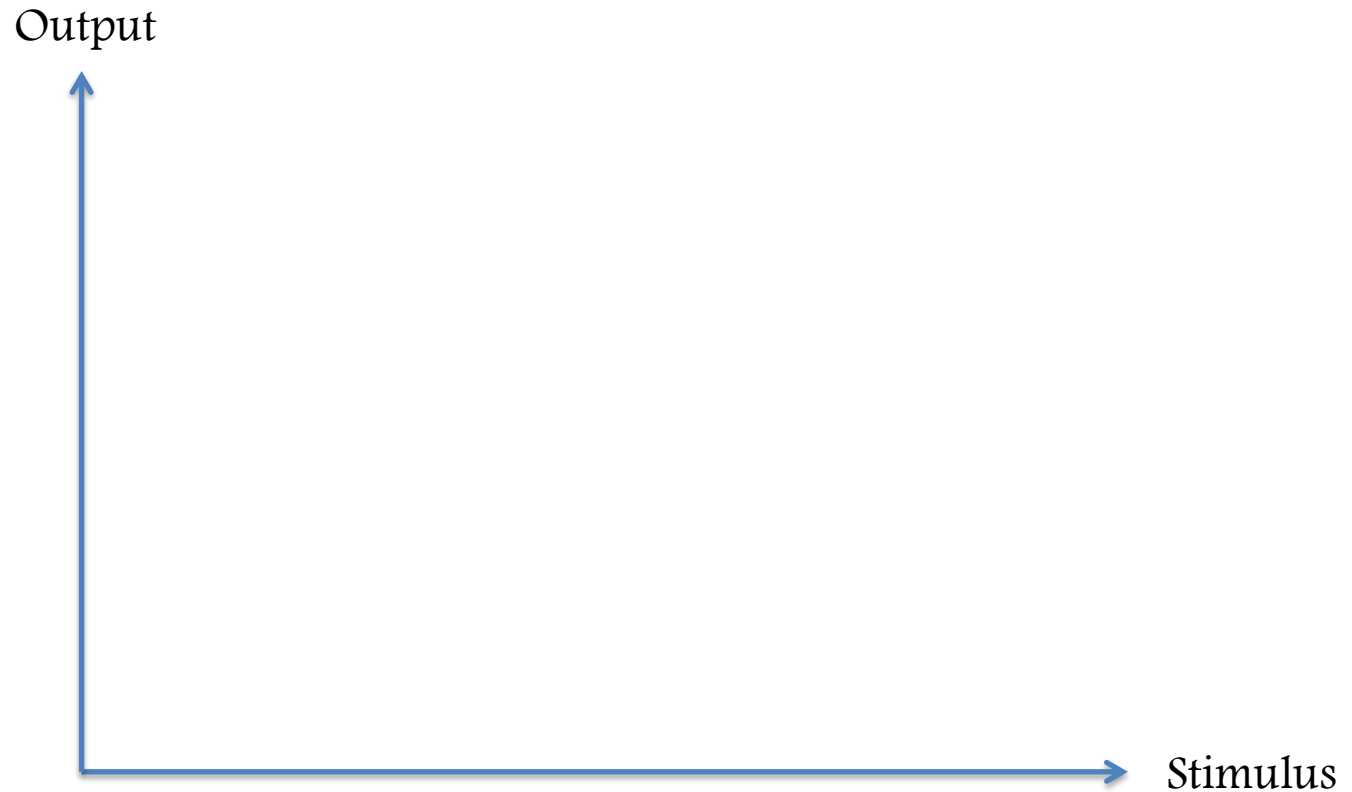
- Capacitive Accelerometer
 - Analog Devices ADXL210
 - Bosch SMB110
 - Crossbow CXL01LF1 (low “g” accelerometer)

- Piezoresistive Accelerometer
 - High Performance Planar Accelerometer
 - (Patridge et al. 2000)



TIME FOR A BREAK!

Sensor Characteristics



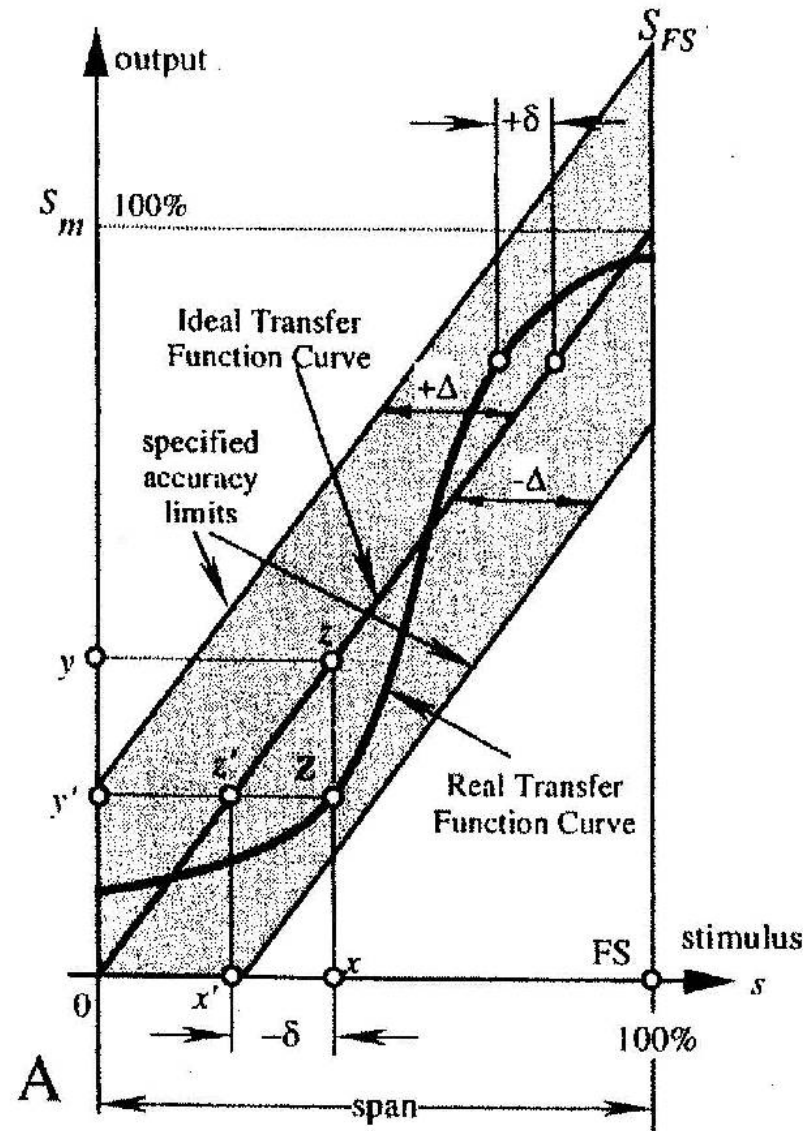
Sensor Characteristics

- Sensitivity

Sensor Characteristics I

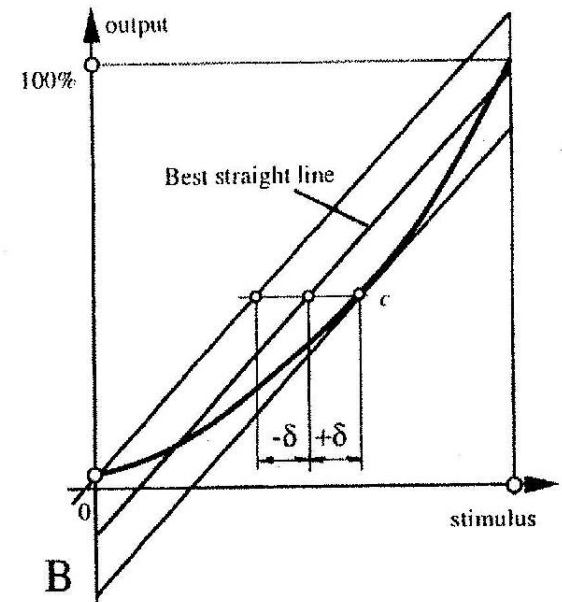
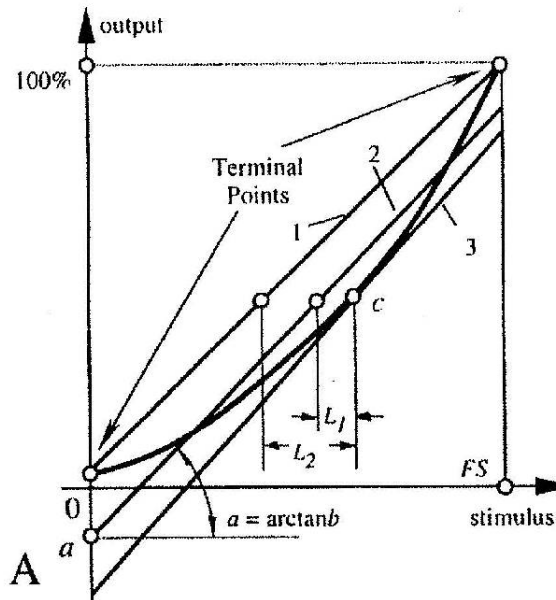
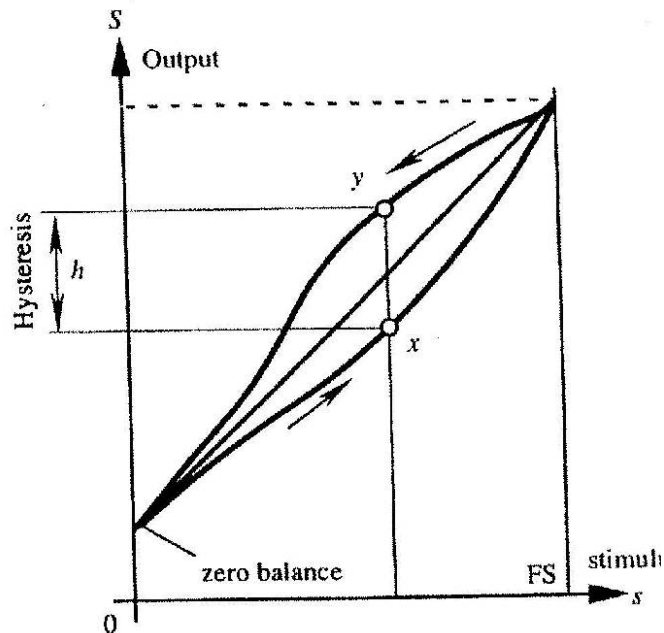
- Here, a sensor is regarded as a black box where we are only concerned with the input and output relationship.
- **Transfer function**: An ideal or theoretical input-output relationship for each sensor. It can be a linear or nonlinear function.
- **Input and output full scales**: A dynamic range of a stimulus or output that is covered by a sensor
- **Error**: The difference between the ideal value and the measurement.
- **Accuracy**: The maximum error between the ideal value and the measured one. They are often represented in terms of (1) measured input value, (2) percent of input span, and (3) output voltage (current) value.

Sensor Characteristics II



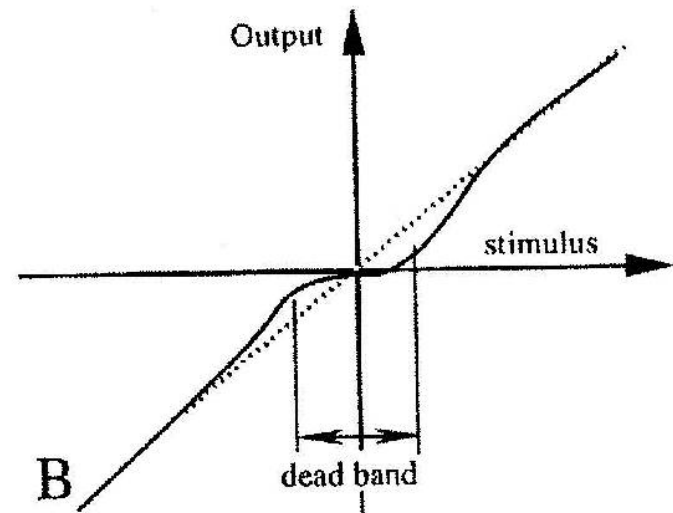
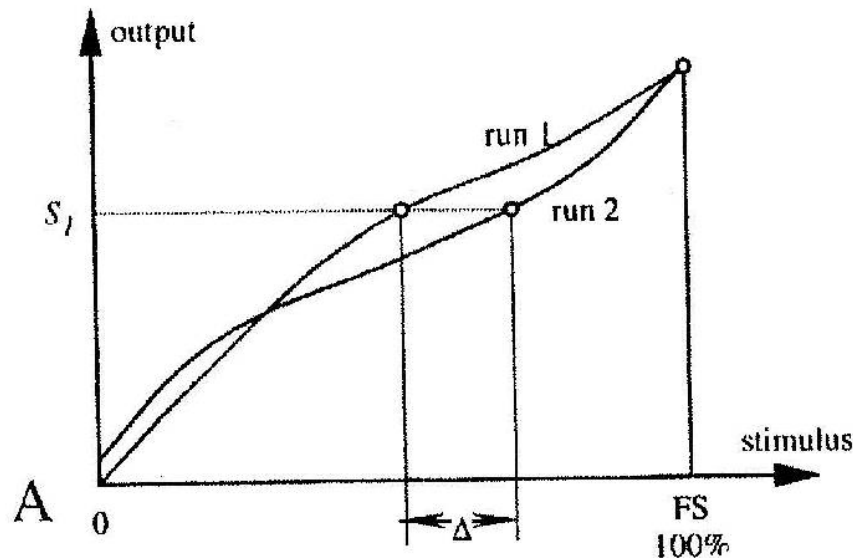
Sensor Characteristics III

- **Hysteresis**: A sensor displays a hysteresis behavior when the sensor response has a directionality. (Primary due to friction and structural change of the sensor materials).
- **Nonlinearity**: A nonlinearity is the maximum deviation of the real transfer function from the approximated straight line.



Sensor Characteristics IV

- **Saturation**: At a certain level of the input stimulus, the output signal become no longer responsive.
- **Repeatability**: The maximum difference between two consecutive readings.
- **Resolution**: the smallest variation of the stimulus that can be sensed at the output level. (There are several different definitions of resolutions, which will be described later on.)



What happens when the stimulus varies over time?

DYNAMIC CHARACTERISTICS

General Classification of Instruments based on Dynamic Characteristics

- Zero order instrument

$$a_0 y(t) = b_0 x(t)$$

- First order instrument

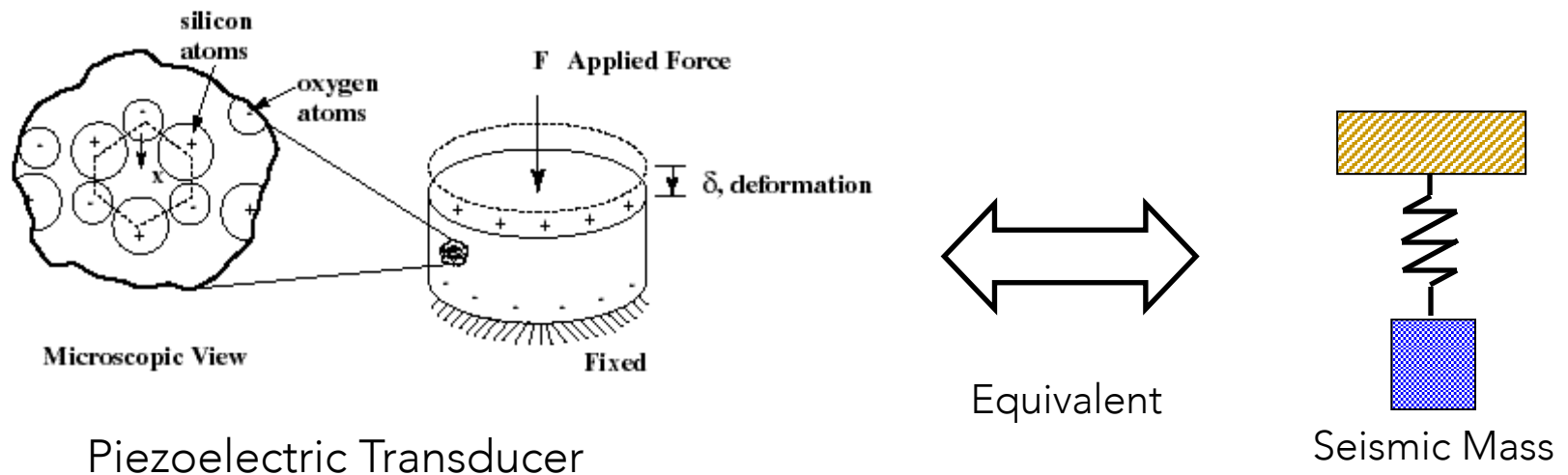
$$a_1 \frac{dy(t)}{dt} + a_0 y(t) = b_0 x(t)$$

- Second order instrument

$$a_2 \frac{d^2 y(t)}{dt^2} + a_1 \frac{dy(t)}{dt} + a_0 y(t) = b_0 x(t)$$

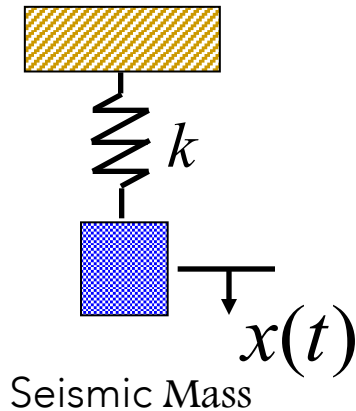
Dynamic Characteristics of Sensor

- Dynamic Characteristics: When an input stimulus varies, a sensor response generally does not follow exactly. This is because both the sensor and the interface circuit have a **dynamic characteristic**.
- Many sensors can be often modeled as a single degree-of-freedom system.
- To understand the dynamic characteristics of a sensor, let's review structural dynamics briefly.



Review of Structural Dynamics I

(1) Free vibration of an undamped system



Equation of motion: $m\ddot{x}(t) + kx(t) = 0$

Solution: $x(t) = A \cos \omega t + B \sin \omega t$

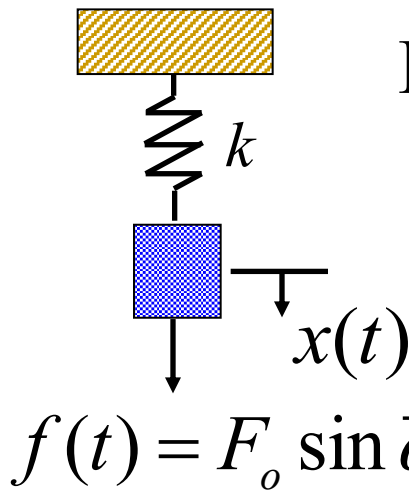
where $\omega = \sqrt{\frac{k}{m}}$: resonance frequency

(2) Free vibration of a damped system

Do it yourself (Refer to any structural dynamics or vibration books)

Review of Structural Dynamics II

(3) Response of an undamped system to harmonic loading



Equation of motion : $m\ddot{x}(t) + kx(t) = F_o \sin \bar{\omega} t$

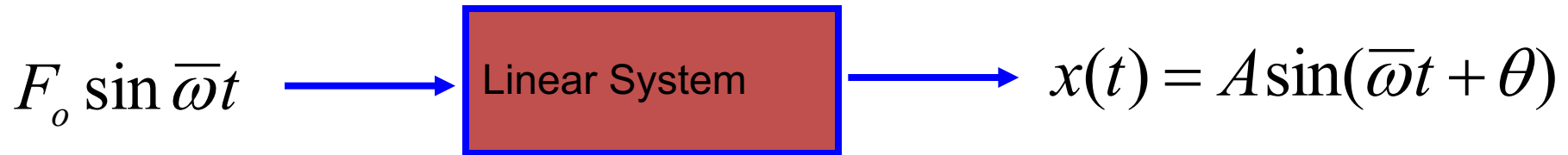
$$\text{Solution : } x(t) = \frac{F_o}{k} \left[\frac{1}{1 - (\bar{\omega}/\omega)^2} \right] \sin \bar{\omega} t$$

(4) Response of a damped system to harmonic loading

Do it yourself (Refer to any structural dynamics or vibration books)

Review of Structural Dynamics III

$$M\ddot{y} + C\dot{y} + Ky = f(t)$$



$$\text{where } A = \frac{F_o}{k} \left[\frac{1}{\sqrt{(1-r^2)^2 + (2\xi r)^2}} \right] \quad \text{and} \quad \tan \theta = \frac{2\xi r}{1-r^2}$$

$$r = \frac{\bar{\omega}}{\omega} \quad \text{and} \quad \xi = \frac{c}{c_{cr}} = \frac{c}{2\sqrt{km}}$$

Back to Dynamic Characteristics of Sensor

- **Frequency band of operation**: describes the frequency range that a sensor operates. Frequency limits are described by lower and higher cut-off frequency.
- **Frequency response** describes how fast and how slowly a sensor can respond to a change in the input stimulus.
- **Time constant**: For you to investigate.
- **Cut-off frequency**: For you to investigate.
- **Resonant frequency**: For you to investigate.

Selection of Accelerometer for Your Application

- What is the frequency range of your application?
- What is the anticipated magnitude of acceleration?
- What is the operating temperature range?
- What level of resolution is required?
- What is the maximum tolerable size?
- Is there intense acoustic electromagnetic or electrostatic field present?
- What kind of power supply is available?
- What is an anticipated overshock?
- What kind of data acquisition system will be used with your accelerometer?
- Is it compatible with your data acquisition system?
- Is it cost effective?

Summary

- We used an accelerometer as an example to study the following
 - Physical principles of sensors
 - How they are operated, fabricated?
 - How to choose the best sensor for your applications?
- Review of structural dynamics
- You should be able to follow similar logical steps to find appropriate sensors for your applications.

The End

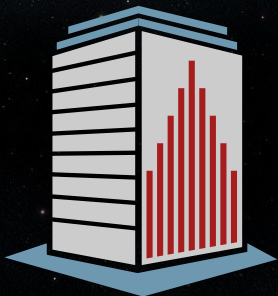
QUESTIONS?



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